

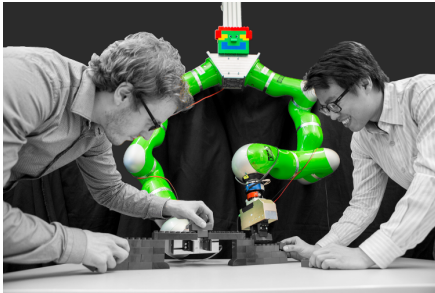
# Legible Action Selection in Human-Robot Collaboration

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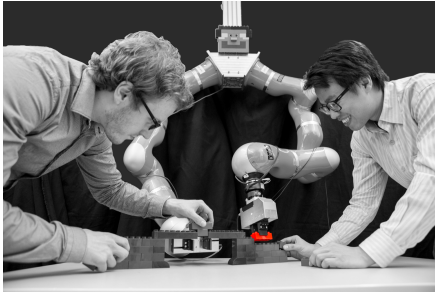
# The Vision - The Adaptive Robot-Co-Worker



The adaptive cobot in an assembly process:

- understand ongoing tasks & human behavior
- select single actions accordingly
- support human co-worker

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The adaptive cobot in an assembly process:

- understand ongoing tasks & human behavior
- select single actions accordingly
- support human co-worker

## Problem formulation

legible action selection given multiple tasks

- estimate human belief in current task
- act supportive when needed

## Requirements for a legible action selection framework

- increase team-efficiency
- supporting actions are taken when needed
- humans accept robot behavior

## Related Work

### Legible Motion Planning in HRC

Match human expectations of an excited trajectory by adjusting the motion, as

- goal-driven actions [Dragan+ 2013b; Dragan+ 2013a]
- obtained from black-box optimization [Stulp+ 2013; Stulp+ 2015]

✗ no task knowledge incorporated

### Human Centered Probabilistic Decision Frameworks in HRC

Sequential decision-making problem as a Markov Decision Processes, e.g.

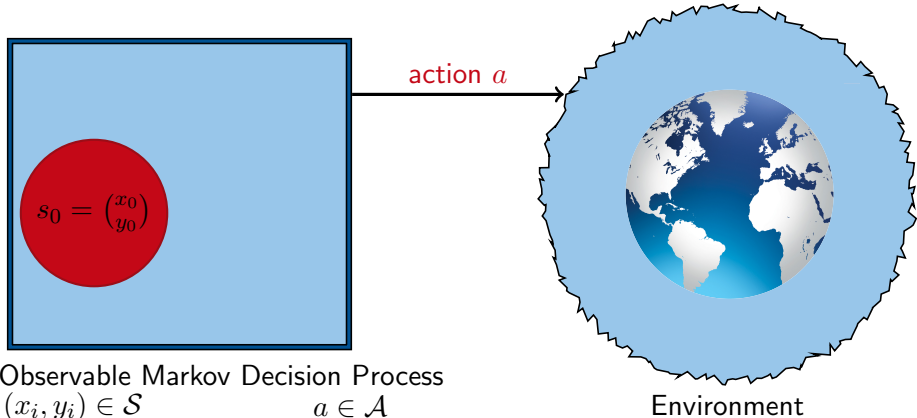
- cost-sensitive action selection based on heuristics [Hoffman+ 2007]
- incorporating human preferences as a single hidden variable [Nikolaidis+ 2015]

✗ no legibility involved

### Contribution

Incorporate legibility in a sequential decision-making problem as a hidden goal Markov Decision Process - **HGMDP**

# Mixed Observable Markov Decision Process



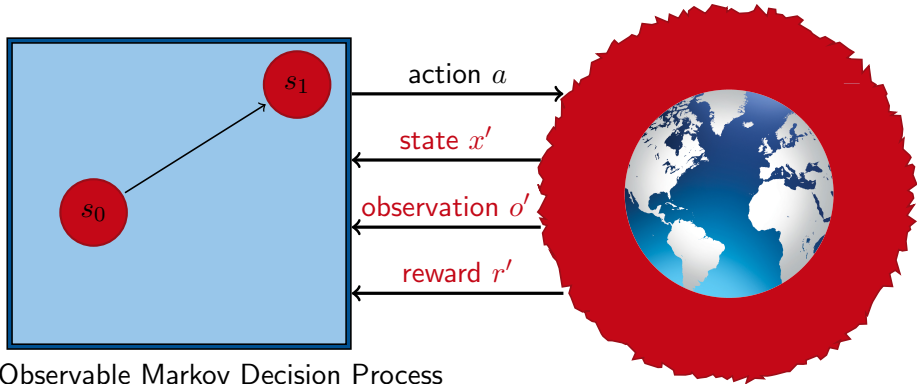
Mixed Observable Markov Decision Process

$$s_i = (x_i, y_i) \in \mathcal{S} \quad a \in \mathcal{A}$$

fully observable state variable  $x \in \mathcal{X}$

hidden state variable  $y \in \mathcal{Y}$

# Mixed Observable Markov Decision Process



Mixed Observable Markov Decision Process

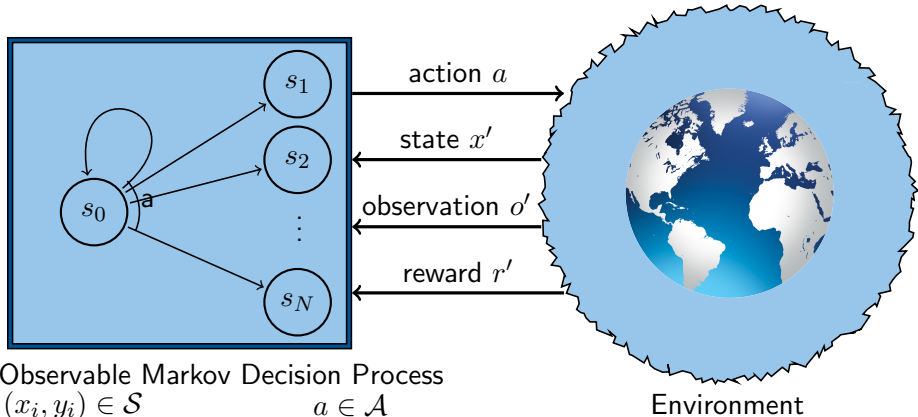
$s_i = (x_i, y_i) \in \mathcal{S}$   $a \in \mathcal{A}$

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Environment

# Mixed Observable Markov Decision Process



Mixed Observable Markov Decision Process

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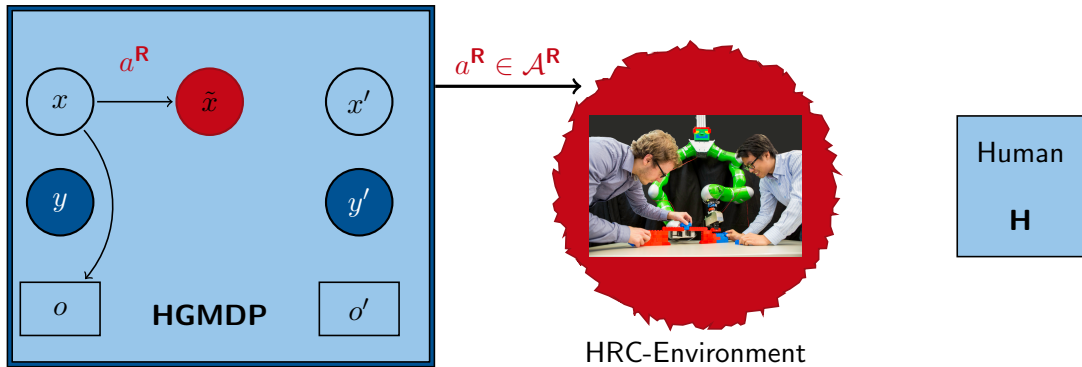
fully observable state variable  $x \in \mathcal{X}$

hidden state variable  $y \in \mathcal{Y}$

# Hidden Goal Markov Decision Process New

Given a sequential decision problem for a human **H** and a robot **R**.

- finite action sets  $\mathcal{A}^R, \mathcal{A}^H$
- **task progress** as fully observable  $\mathcal{X}$
- **human belief in the goal** as hidden state  $\mathcal{Y}$

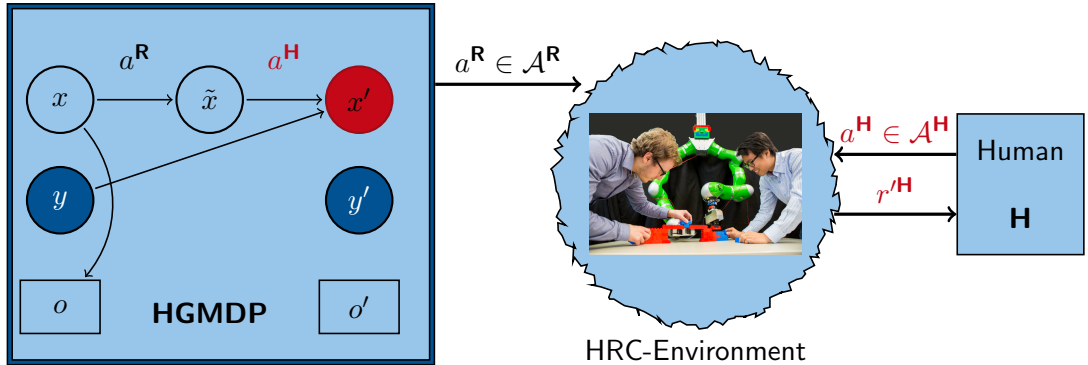




# Hidden Goal Markov Decision Process New

Given a sequential decision problem for a human **H** and a robot **R**.

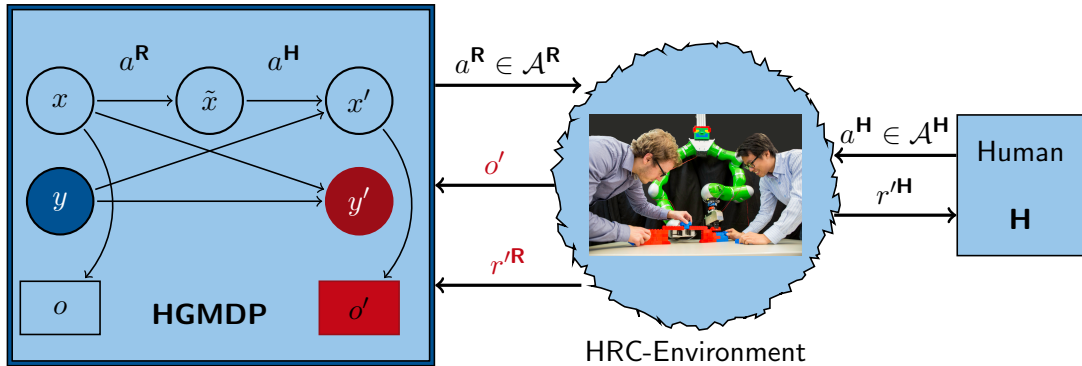
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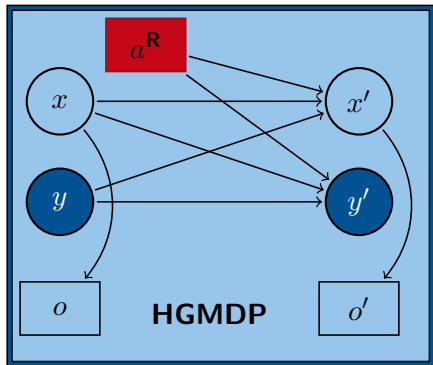
# Hidden Goal Markov Decision Process New

Given a sequential decision problem for a human **H** and a robot **R**.

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# Human Belief Update



We assume

- the robot acts deterministically in  $\mathcal{X}$
- $\mathbf{H}$  follows a stochastic policy  $\pi^{\mathbf{H}}(\tilde{x}, y, a^{\mathbf{H}})$
- conditional independence  $x' \perp\!\!\!\perp y'$

dynamic Bayesian Network modelling the relation of  $a^R$  to Human belief update:

$$\mathbb{P}(y'|x, y, a^R) \propto \mathbb{P}(a^R|x, y)\mathbb{P}(y'|x)$$

# Approximatively Solving HGMDP

Solving **HGMDP** exactly is PSPACE-complete!

## Approximative solution

1. feature based state aggregation by mapping single actions to task sets
2. evaluate human belief at every step
  - if **H**'s belief is correct ( $y = y^*$ ), solve MDP for  $y^*$
  - select strongest belief of **H** ( $y_i \neq y^*$ ), solve MDP  $M_i$
3. abstracted MDP  $M_i$  for false belief of the human
  - states given as  $\mathcal{S} = \{\mathcal{X}, y^*, y_i\}$
  - following legible reward model

$$R_{L,i}(x, y_i, a^{\mathbf{R}}) = \mathbb{P}(y^*|x, y_i, a^{\mathbf{R}}) - \lambda \mathbb{P}(y_i|x, y_i, a^{\mathbf{R}})$$

# Experimental Setup

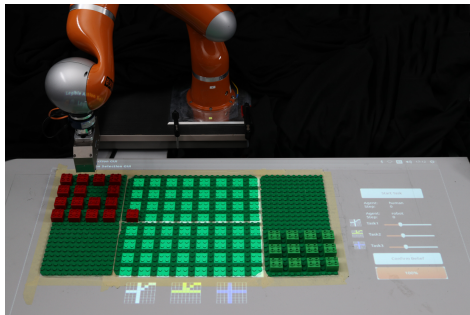


(a) Scenario 1

(b) Scenario 2

## Main experimental setup

- 2 pick-and-place assembly scenarios
- 3 task goals for each scenario
- $n = 10$  participants
- 18 repetitions each



LEGO-assembly scenario with the goal being unknown to the human collaborator **H**.

# Experimental Setup

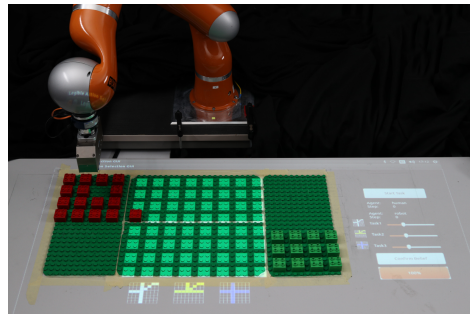


(a) Scenario 1

(b) Scenario 2

## Compared policies

- **Efficient**, i.e. shortest distance (**E**)
- **HGMDP** policy (**L**)
- **HGMDP** policy with direct belief feedback (**LF**)



LEGO-assembly scenario with the goal being unknown to the human collaborator **H**.

# Experimental Results - Subjective Evaluation

Confirmed Hypotheses: Compared to policy E, participants will rate the robot's actions in the HGMDP

H1 ... more helpful.

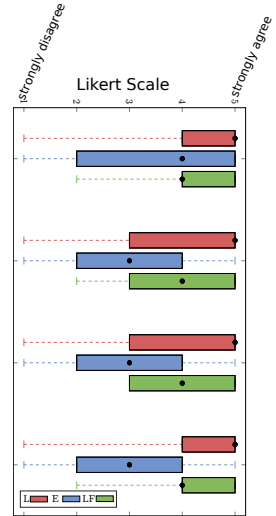
H2 ... more responsive.

Q1 *The robot was acting **efficiently**.*

Q2 *The robot **adapted** the strategy when I was in doubt about the task.*

Q3 *The robot **reacted** when I made errors.*

Q4 *The choice of actions of the robot was **helpful**.*



# Experimental Results - Subjective Evaluation

**Confirmed Hypotheses: Compared to policy E, participants will rate the robot's actions in the HGMDP**

**H1** ... more helpful. (Q1,)Q4 → ✓

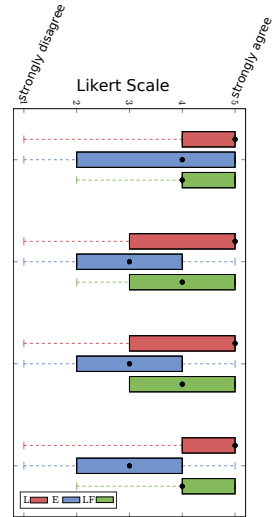
**H2** ... more responsive. Q2, Q3 → ✓

**Q1** *The robot was acting **efficiently**.*

**Q2** *The robot **adapted** the strategy when I was in doubt about the task.*

**Q3** *The robot **reacted** when I made errors.*

**Q4** *The choice of actions of the robot was **helpful**.*





# Experimental Results - Empirical Evaluation

Claimed Hypotheses: By applying HGMDP,

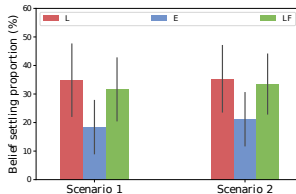
**H3** ... **H**'s belief converges faster to the correct goal.

(supportive agent)

**H4** .. the overall error-rate decreases.

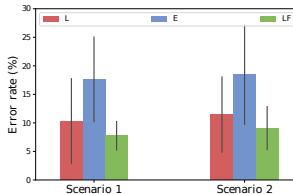
(productivity)

Belief settling proportion



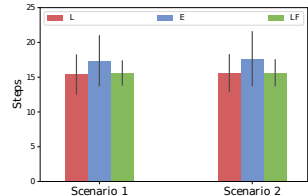
✓ confirming **H3**

Error rate



✓ confirming **H4**

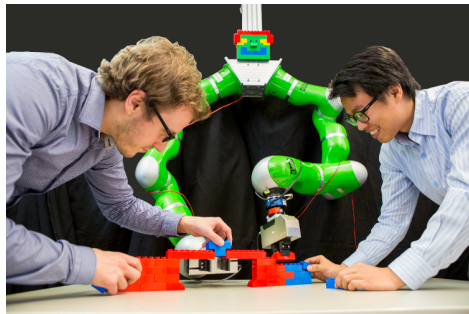
Number of task completion steps



# Summary

## Conclusion

- outline of **HGMDP**- a sequential and adaptive decision-making framework
- online estimation of human belief
- confirmed four hypothesis in user-study
- distinct improvements in subjective feedback
- increased empirical performance measures



# References



A Dragan and S Srinivasa. **Generating Legible Motion.** In: *Robotics: Science and Systems* (2013).

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In: *IEEE Trans. Robot.* 23 (2007), pp. 952–961.



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**Efficient Model Learning from Joint-Action Demonstrations for Human-Robot Collaborative Tasks.** In: *HRI*. 2015, pp. 189–196.

F Stulp, J Grizou, B Busch and M Lopes. **Facilitating Intention Prediction for Humans by Optimizing Robot Motions.** In: *IROS*. 2015.

F Stulp and O Sigaud. **Policy Improvement: Between Black-Box Optimization and Episodic Reinforcement Learning.** In: *JFPDA*. 2013.



# Additional Information & Material

# Experimental Results - Subjective Evaluation

**Confirmed Hypotheses:** Compared to policy E, participants will rate the robot's actions in the HGMDP

**H1** ... more helpful.

**H2** ... more responsive.

Wilcoxon signed-rank test results

- Q1    *The robot was acting efficiently.*  
Q2    *The robot adapted the strategy when I was in doubt about the task.*  
Q3    *The robot reacted when I made errors.*  
Q4    *The choice of actions of the robot was helpful.*

Question	Overall Comparison	L vs E	L vs LF	E vs LF
Q1	0.0009	0.0013	0.8591	0.0004
Q2	< 0.0001	< 0.0001	0.2789	0.0002
Q3	< 0.0001	< 0.0001	0.5525	< 0.0001
Q4	< 0.0001	< 0.0001	0.8552	< 0.0001

# Feature Based State Aggregation

## General Assembly Scenario

Given  $M$  tasks  $\mathcal{T} = \{T_1, T_2 \dots T_M\}$ , there exists

- a set of all task components  $\mathcal{C} = \bigcup_{i=1}^{|\mathcal{T}|} T_i$
- a set tasks  $\mathcal{P}_i = \{T_j | c_i \in T_j\}$  each components belongs to

## State Aggregation

Defining an equivalence relation over  $\mathcal{C}$  and  $\mathcal{P}$

$$\mathcal{R} = \left\{ (c_m, c_n) | \mathcal{P}_m = \mathcal{P}_n \quad c_m, c_n \in \mathcal{C} \right\}$$

$$\Pi = \{[c]_{\mathcal{R}} | c \in \mathcal{C}\}$$

obtains the final state aggregation by an additional error-counter  $\varphi_e(x)$ :

$$\Phi(x) : x \mapsto |\Pi \cap T_x| \mapsto [\varphi_e(x), \varphi_1(x), \varphi_2(x), \dots, \varphi_{|\Pi|}(x)]^T$$



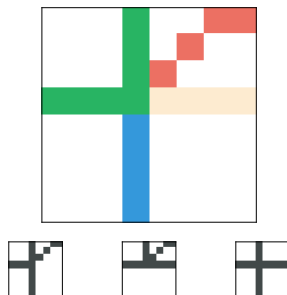
# Example State Aggregation

## State aggregation - Scenario 1

- $\mathcal{T} = \{T_1, T_2, T_3\}$  tasks
- $\mathcal{C} = \{c_1, c_2 \dots c_{19}\}$  legal positions
- $\mathcal{P} = \{P_1, P_2, P_3, P_4\}$  task mappings shown in green, blue, red and beige
- $|E| = \{7, 4, 4, 4\}$  maximum counter per set  $P_i$
- $|\varphi_e(x)| \leq 4$  error counter

Define a mapping of single task components to tasks:

$$\Phi(x) : x \mapsto [\varphi_e(x), \varphi_1(x), \varphi_2(x), \varphi_3(x), \varphi_4(x)]^T$$



(c) Scenario 1

# Transition Probability Functions

We assume that **H** always acts greedily according to her goal expectation

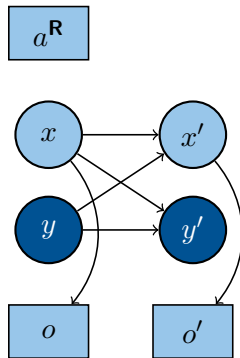
$$\pi^{\mathbf{H}}(x, y, a^{\mathbf{H}}) \propto \exp(\beta_2 R^{\mathbf{H}}(x, y, a^{\mathbf{H}}))$$

The robot acts deterministically such that

$$T_X(x, y, a^{\mathbf{R}}, x') = \mathbb{P}(x'|x, y, a^{\mathbf{R}}) = \pi^{\mathbf{H}}(\tilde{x}, y, a^{\mathbf{H}})$$

As shown in the DBN that  $x' \perp\!\!\!\perp y'$  holds, such that

$$T_Y(x, y, a^{\mathbf{R}}, x', y') = \mathbb{P}(y'|x, y, a^{\mathbf{R}})$$





# Transition Probability Functions

We assume that **H** always acts greedily according to her goal expectation

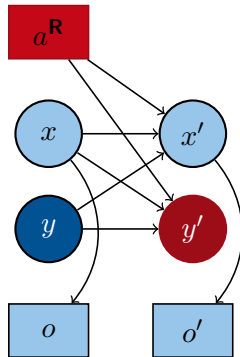
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$$T_Y(x, y, a^{\mathbf{R}}, x', y') = \mathbb{P}(y'|x, y, a^{\mathbf{R}})$$



# Goal Inference

The goal inference in **HGMDP** is obtained from the distribution of  $y$  at each transition according to

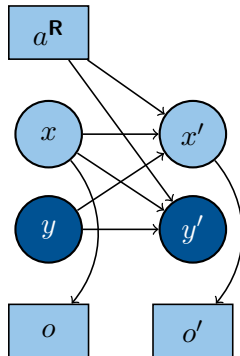
$$b'(y') \propto \mathbb{P}(o|x', y', a^{\mathbf{R}}) \sum_y T_{XY}(x, y, a^{\mathbf{R}}, x', y') b(y)$$

The observation is modeled deterministically

$$\mathbb{P}(o|x', y', a^{\mathbf{R}}) = \begin{cases} 1, & \text{if } o = a^{\mathbf{H}} \\ 0, & \text{otherwise} \end{cases} \quad (1)$$

The state transition function is given by

$$T_{XY}(x, y, a^{\mathbf{R}}, x', y') = \pi^{\mathbf{H}}(\tilde{x}, y, a^{\mathbf{H}}) \mathbb{P}(y'|x, y, a^{\mathbf{R}})$$



# Incorporating Legibility in Reward Model

Human inference probability for  $\mathbf{R}$ 's actions:

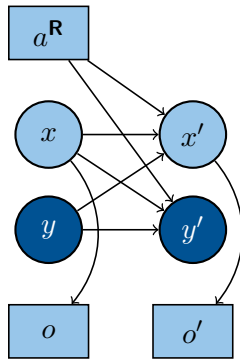
$$\mathbb{P}(a^{\mathbf{R}}|x, y) \propto \exp(\beta_1 R^{\mathbf{R}}(x, y, a^{\mathbf{R}}))$$

Given the actual goal  $y^*$ , the legible reward model results in:

$$R_{\mathbf{L}}(x, y, a^{\mathbf{R}}) = \mathbb{P}(y^*|x, y, a^{\mathbf{R}}) - \lambda \sum_{y' \in \mathcal{Y} \setminus \{y^*\}} \mathbb{P}(y'|x, y, a^{\mathbf{R}})$$

In return, this results in the following update rule for  $\mathbf{H}$ 's belief:

$$\mathbb{P}(y'|x, y, a^{\mathbf{R}}) \propto \begin{cases} p_c \mathbb{P}(y'|x, a^{\mathbf{R}}), & \text{if } y = y' \\ \frac{1-p_c}{|\mathcal{Y}|-1} \mathbb{P}(y'|x, a^{\mathbf{R}}), & \text{otherwise} \end{cases}$$



## Approximatively Solving HGMDP

Approximate **HGMDP** based on the current human belief  $y$  by a fully observable MDP  $M_i$  with  $\mathcal{S} = \{\mathcal{X}, y^*, y_i\}$  and

$$T_i = \mathbb{P}(x', y' | x, y, a^{\mathbf{R}}) = \begin{cases} \pi^{\mathbf{H}}(\tilde{x}, y_i, a^{\mathbf{H}}), & \text{if } y' = y_i \\ 0, & \text{if } y' \neq y_i \end{cases}$$

as well as

$$R_{\mathbf{L},i}(x, y_i, a^{\mathbf{R}}) = \mathbb{P}(y^* | x, y_i, a^{\mathbf{R}}) - \lambda \mathbb{P}(y_i | x, y_i, a^{\mathbf{R}})$$

### Obtain HGMDPPolicy

Resulting in the overall policy to solve **HGMDP**

$$\pi_{\mathbf{L}}(x, b(y), a^{\mathbf{R}}) = \begin{cases} \pi^*(M_i(\mathcal{S} := \mathcal{X})) & \text{if } \arg \max b(y) = y^* \\ \hat{\pi}_{\mathbf{L}}(x, \arg \max_{y \in \mathcal{Y} \setminus \{y^*\}} b(y), a^{\mathbf{R}}) & \text{else} \end{cases}$$



# General Approach - Hidden Goal Markov Decision Process

## Problem Definition

Given a sequential decision problem for a human **H** and a robot **R**.

- Finite action sets  $\mathcal{A}^{\mathbf{R}}, \mathcal{A}^{\mathbf{H}}$ .
- Reward functions given as  $R^{\mathbf{R}}, R^{\mathbf{H}}, \dots$ .
- Obtain  $a^{\mathbf{R}} = \operatorname{argmax} \sum_i^N R$ .

## Hidden Goal Markov Decision Process

Given as  $M = (\mathcal{X}, \mathcal{Y}, I_Y, \mathcal{A}^{\mathbf{R}}, \mathcal{A}^{\mathbf{H}}, \mathcal{O}, T_X, T_Y, Z, R^{\mathbf{R}}, R^{\mathbf{H}}, R_{\mathbf{L}}, \gamma, y^*)$ .

- $\mathcal{X}$ : fully observable task state.
- $\mathcal{Y}$ : hidden variable representing human goal expectation ( $y^*$  as the actual goal).
- $\mathcal{O}$ : set of observations, given as the actual human action.
- $T_X = \mathbb{P}(x'|x, y, a^{\mathbf{R}})$  and  $T_Y = \mathbb{P}(y'|x, y, a^{\mathbf{R}}, x')$ : transition probability functions.
- $Z$ : probability distribution to observe  $o$ .
- $\gamma$ : discount factor  $\in [0, 1]$ .



# Hypotheses and Measurements

## Claimed Hypotheses

Compared to the *efficient* policy, Participants will rate the robot's actions in the **HGMDP**...

**H1** more helpful.

**H2** more responsive.

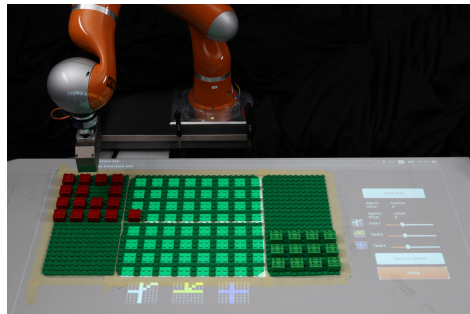
By applying the **HGMDP**, ...

**H3** **H**'s belief converges faster to the correct goal.

**H4** the overall error-rate decreases.

## Experimental Measurements

- subjective questionnaire (**H1**, **H2**)
- belief settling proportion, w.r.t. to steps (**H3**)
- error-rate over all runs (**H4**)



LEGO-assembly scenario with the goal being unknown to the human collaborator **H**.

# Outsourced